

# **Discrete Mathematics**

## **Logic and Proof**

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# Conditional Propositions

## The Conditional Proposition $p \rightarrow q$

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- › Truth table.

## Variations of $p \rightarrow q$

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